

Heat Transfer

Computational Laboratories

Heat Exchangers (Laboratory IV)

Understanding the role of physical parameters and operating conditions on the thermal design and performance of heat exchangers

Heat Exchangers (HXs) - Introduction

Heat Exchangers

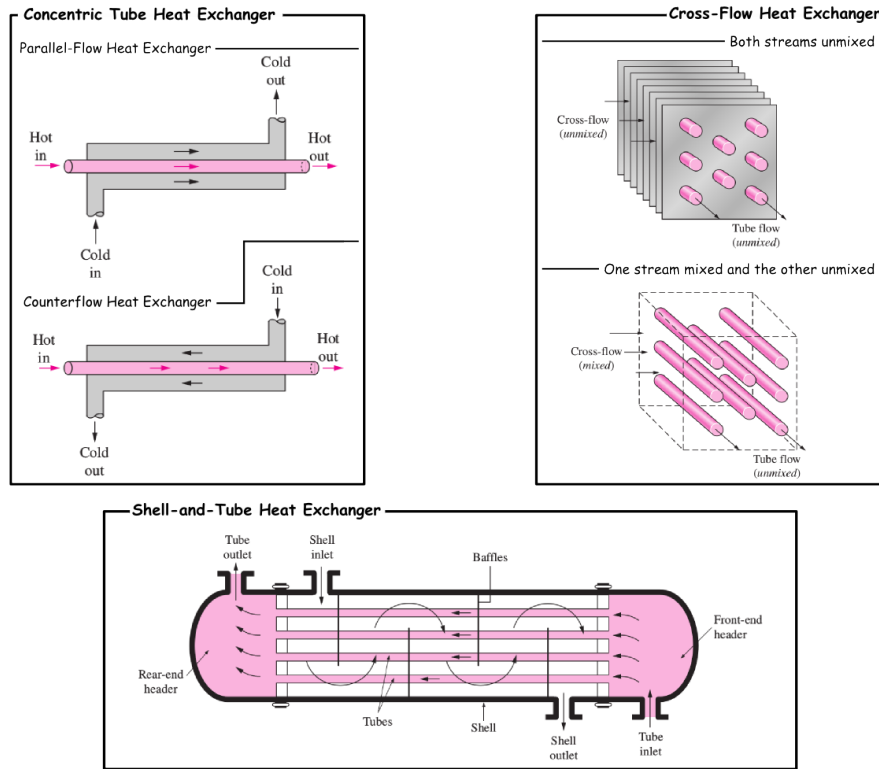
Heat exchangers are devices that promote heat exchange between two fluids that are at different temperatures, preventing at the same time their mixing.

The hot and cold fluid streams are separated by wall or are provided to the heat exchanger at different time instants (static-type regenerative).

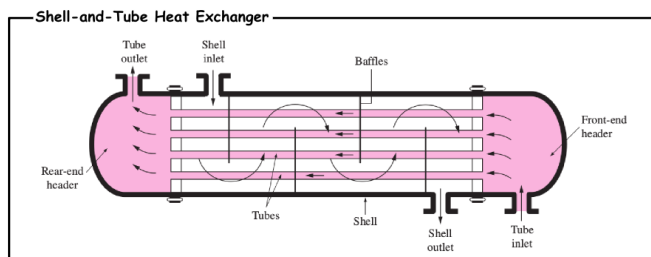
Applications

- Power production
- Air-conditioning
- Waste heat recovery
- Chemical process industry

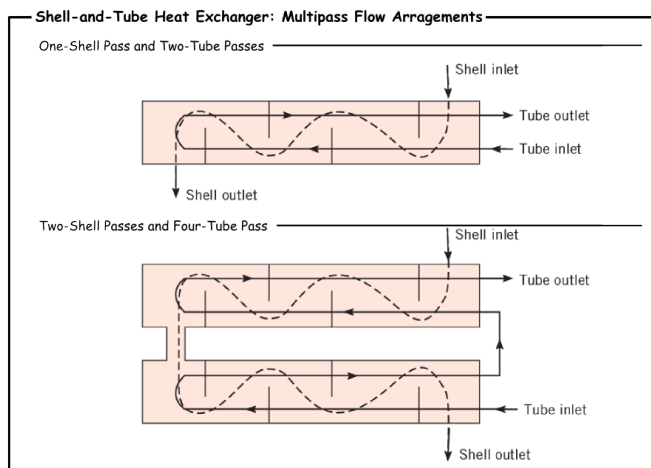
Types of Heat Exchangers (1/2)



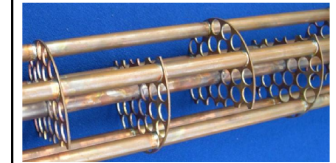
Types of Heat Exchangers (2/2): Shell-and-Tube HX



HX in Exhibition - South Tower (Atrium)

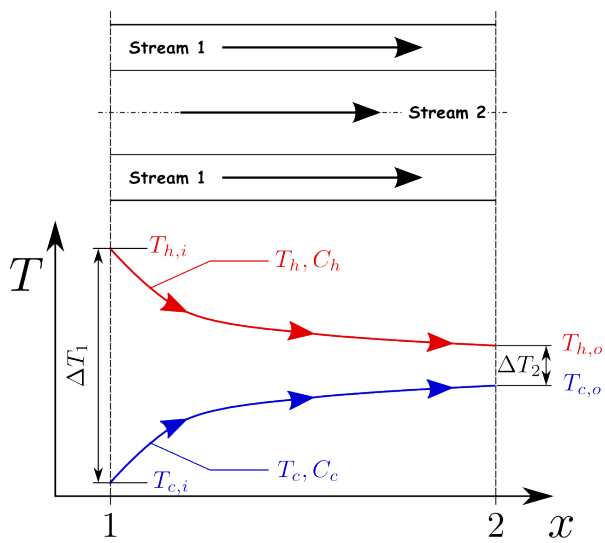


Baffles: detailed view

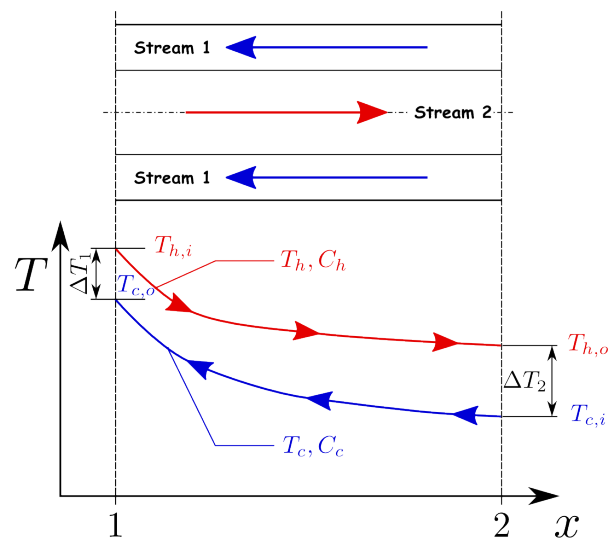


Temperature Distributions in Concentric Tube HXs

Parallel-Flow Heat Exchanger



Counterflow Heat Exchanger



T - Temperature; C - heat capacity rate ($= \dot{m}c_p$); h - hot fluid; c - cold fluid; i - inlet; o - outlet.

Heat Exchanger Analysis and Methods

Heat Exchanger Design (LMTD or ε -NTU methods)

Determination of the **heat exchanger type** and **size** (A - total heat transfer surface area) for prescribed:

- hot and cold mass flow rates (\dot{m}_h and \dot{m}_c);
- inlet temperatures of the hot and cold fluid streams ($T_{h,i}$ and $T_{c,i}$);
- desired outlet temperature for the hot or cold fluid ($T_{h,o}$ or $T_{c,o}$).

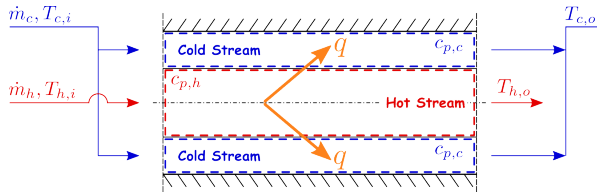
Heat Exchanger Performance (ε -NTU method)

Determination of the **rate of heat transfer** (q) and **fluid outlet temperatures** ($T_{c,o}$ and $T_{h,o}$) for prescribed:

- heat exchanger type;
- heat exchanger size (A);
- hot and cold mass flow rates (\dot{m}_h and \dot{m}_c);
- inlet temperatures of the hot and cold fluid streams ($T_{h,i}$ and $T_{c,i}$).

Total Heat Transfer Rate

The **total heat transfer rate from the hot to the cold fluid stream** can be obtained by performing an overall energy balance for the hot or cold fluids.



- For the hot fluid stream:

$$q = \underbrace{\dot{m}_h c_{p,h}}_{C_h} (T_{h,i} - T_{h,o})$$

- For the cold fluid stream:

$$q = \underbrace{\dot{m}_c c_{p,c}}_{C_c} (T_{c,o} - T_{c,i})$$

The total heat transfer rate can also be obtained through a **modified form of the Newton's Law of cooling** as follows[†]:

$$q = UA\Delta T_{lm}$$

where,

U - overall heat transfer coefficient;
 A - total heat transfer surface area;
 ΔT_{lm} - Log mean temperature difference (LMTD). Equivalent to a mean temperature difference between two fluids for the entire heat exchanger.

[†]This procedure to evaluate q corresponds to the LMTD Method.

Log Mean Temperature Difference: Single-Pass Heat Exchangers (Concentric Tube and Shell-and-Tube)

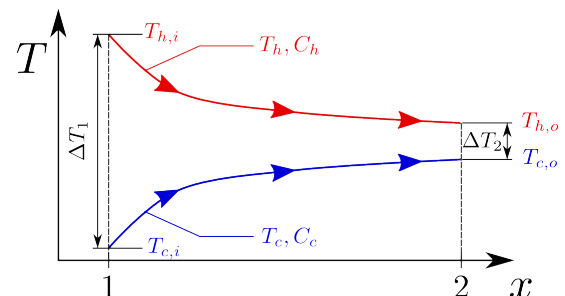
$$\Delta T_{lm} = \frac{\Delta T_1 - \Delta T_2}{\ln(\Delta T_1 / \Delta T_2)}$$

$$\Delta T_1 = T_{h,1} - T_{c,1} = \begin{cases} T_{h,i} - T_{c,i} & \text{PF HX} \\ T_{h,i} - T_{c,o} & \text{CF HX} \end{cases}$$

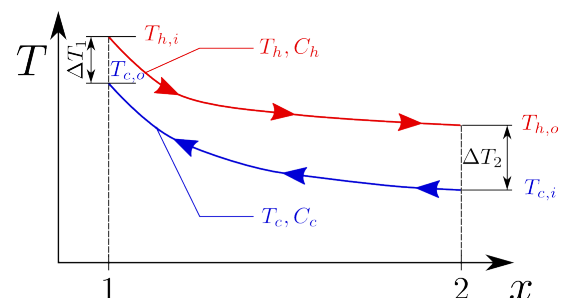
$$\Delta T_2 = T_{h,2} - T_{c,2} = \begin{cases} T_{h,o} - T_{c,o} & \text{PF HX} \\ T_{h,o} - T_{c,i} & \text{CF HX} \end{cases}$$

For specified inlet and outlet temperatures ($T_{h,i}$, $T_{c,i}$, $T_{h,o}$ and $T_{c,o}$) the log mean temperature difference for a counterflow heat exchanger is always greater than that for a parallel-flow heat exchanger, i.e., $\Delta T_{lm,CF} > \Delta T_{lm,PF}$.

Parallel-Flow (PF) Heat Exchanger



Counterflow (CF) Heat Exchanger



Log Mean Temperature Difference: Multipass Shell-and-Tube and Cross-Flow Heat Exchangers (1/2)

- The LMTD as defined previously is limited to concentric tube HXs and single-pass shell-and-tube HXs.
- For multipass and cross-flow heat exchangers a mean temperature difference can also be defined as a function of the LMTD for a counterflow HX as follows:

$$\Delta T_{lm,c} = F \Delta T_{lm,CF}$$

where F is a **correction factor** that depends on the HX type and the inlet and outlet temperatures.

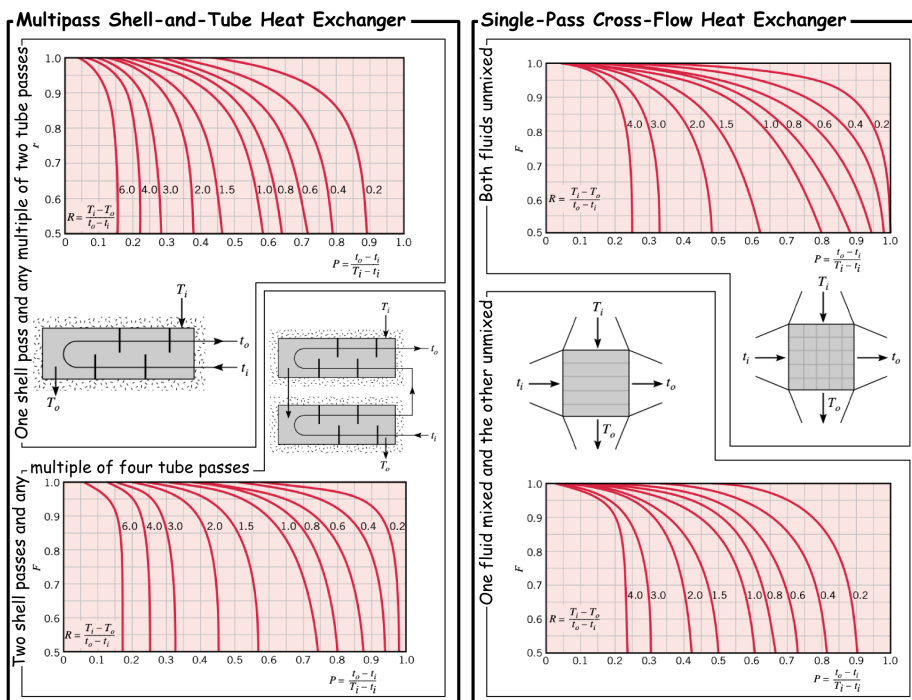
- $F = f(\text{HX geometry}, P, R)$ and is commonly given in charts. P and R are the following temperature ratios:

$$P = \frac{t_2 - t_1}{T_1 - t_1}$$

$$R = \frac{T_1 - T_2}{t_2 - t_1} = \frac{(\dot{m}C_p)_{\text{Tube side}}}{(\dot{m}C_p)_{\text{Shell side}}}$$

- $F \leq 1$

Log Mean Temperature Difference: Multipass Shell-and-Tube and Cross-Flow Heat Exchangers (2/2)



- $P = \frac{t_2 - t_1}{T_1 - t_1}$
 - $0 \leq P \leq 1$
- $R = \frac{T_1 - T_2}{t_2 - t_1}$
 - $0 \leq R \leq \infty$
 - $R = 0$ - Phase change on the shell side
 - $R \rightarrow \infty$ - Phase change on the tube side
- $F = 1$ for a condenser or a boiler

Overall Heat Transfer Coefficient

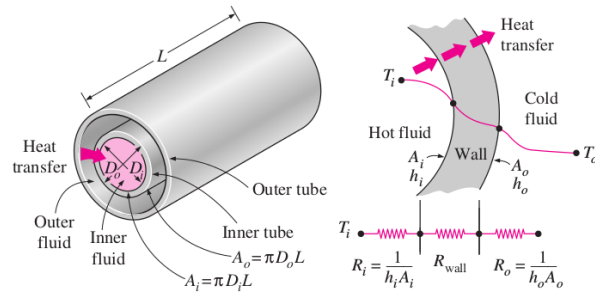
- For a finned surface with a layer of deposits that represents an additional heat transfer resistance (R_f'') the total heat transfer resistance is given by:

$$R_{t,total} = \frac{1}{UA} = \frac{1}{U_c A_c} = \frac{1}{U_h A_h} = \frac{1}{(\eta_o h A)_c} + \frac{R_{f,c}''}{(\eta_o A)_c} + R_w + \frac{R_{f,h}''}{(\eta_o A)_h} + \frac{1}{(\eta_o h A)_h}$$



- For an unfinned concentric tube HX without fouling (clean surfaces) the overall heat transfer coefficient can be obtained as follows

$$\frac{1}{UA} = \frac{1}{U_i A_i} = \frac{1}{U_o A_o} = \frac{1}{(hA)_i} + \underbrace{\frac{\ln(D_o/D_i)}{2\pi kL}}_{R_w} + \frac{1}{(hA)_o}$$



Effectiveness-NTU Method (1/3)

- The **heat transfer effectiveness** (ϵ) is defined as:

$$\epsilon = \frac{q}{q_{max}}$$

where q is the **actual rate of heat transfer** and q_{max} is the **maximum possible heat transfer rate** give by:

$$q_{max} = C_{min} (T_{h,i} - T_{c,i})$$

C_{min} corresponds to the **minimum heat capacity rate** as follows:

$$C_{min} = \text{Min}(C_h, C_c)$$

- For each exchanger the heat transfer effectiveness can be obtained through proper relations:

$$\epsilon = f\left(NTU, \frac{C_{min}}{C_{max}}\right)$$

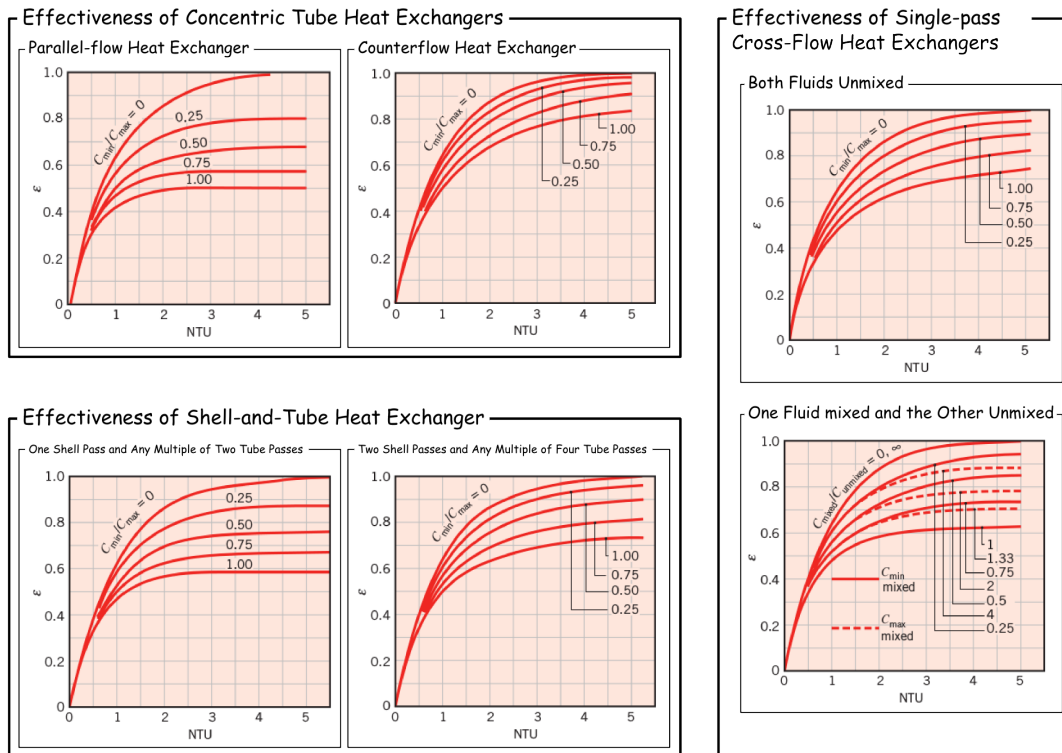
NTU corresponds to the **number of transfer units** and is given by:

$$NTU = \frac{UA}{C_{min}}$$

- NTU can be obtained through relations of the form:

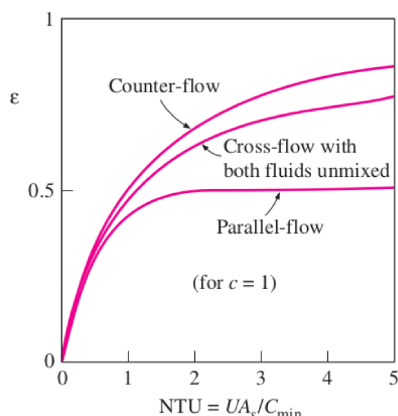
$$NTU = f\left(\epsilon, \frac{C_{min}}{C_{max}}\right)$$

Effectiveness-NTU Method (2/3)

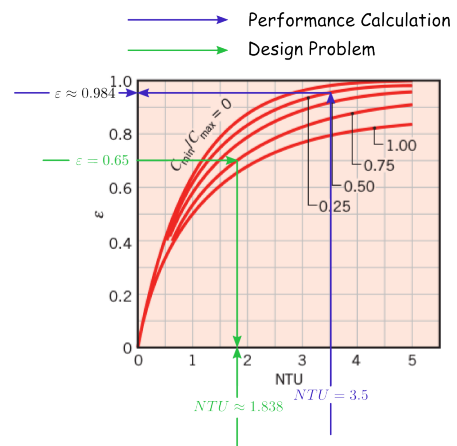


Effectiveness-NTU Method (3/3)

- For performance calculations, effectiveness relations ($\epsilon = f(NTU, C_r)$) are employed whereas for design purposes, NTU relations ($NTU = f(\epsilon, C_r)$) are considered.
- For a boiler or condenser ($C_r (= \frac{C_{min}}{C_{max}}) = 0$) ϵ is independent of the heat exchanger type and flow arrangement, *i.e.*, all heat exchangers have the same effectiveness value.



- For $C_r > 0$ and $NTU \gtrsim 0.25$ the counterflow heat exchanger is the most effective.
- For any HX $C_r = 0$ and $C_r = 1$ corresponds to the maximum and minimum effectiveness values.



Exploring the Software - The Interface (1/2)

Output - Results

Temperature Distributions

Temp vs Distance (0.0 to 1.0). Shell (red line), Tube-CF (green line).

Design Data:

- Overall HT Coeff x Area (UA) = 0,97
- Log-Mean Temp Diff (LMTD) = 0,577
- Q based on LMTD = 0,56
- Q based on Shell Fluid T-Diff = 0,55
- Q based on Tube Fluid T-Diff = 0,55
- R = (TSin-TSout) / (Ttout-TTin) = 2,000
- P = (Ttout-TTin) / (TSin-TTin) = 0,275

Performance Data:

- Effectiveness = Q / Qmax = 0,550
- NTU = UA / Cmin = 0,973
- Cmin / Cmax = 0,500

Input Data

Heat Capacity Rates:

- Shell = 1,0 (Hot)
- Tube = 2,0 (Cold)

Calculation Method:

- Design (LMTD)
- Performance (Effectiveness-NTU)

Desired Shell Outlet Temp: 0,45

Configuration:

- Shell-and-Tube

Temperature Option:

- Dimensional
- NonDim

New Configuration:

- Concentric Tube
- Shell-and-Tube
- Custom Layout

Calculation Method:

- Design (LMTD)
- Performance (Effectiveness-NTU)

Overall HT Coeff x Area (UA): 0,45

Non-dimensional Temperature

$$T^* = \frac{T - T_{c,i}}{T_{h,i} - T_{c,i}}$$

Required Input for "Dimensional" Temp. Option

Exploring the Software - The Interface (2/2)

$T^* = \frac{T - T_{c,i}}{T_{h,i} - T_{c,i}}$

Temperature Distributions

Temp vs Distance (0.0 to 1.0). Shell (red line), Tube-CF (green line).

Design Data:

- Overall HT Coeff x Area (UA) = 0,97
- Log-Mean Temp Diff (LMTD) = 0,577
- Q based on LMTD = 0,56
- Q based on Shell Fluid T-Diff = 0,55
- Q based on Tube Fluid T-Diff = 0,55
- R = (TSin-TSout) / (Ttout-TTin) = 2,000
- P = (Ttout-TTin) / (TSin-TTin) = 0,275

Performance Data:

- Effectiveness = Q / Qmax = 0,550
- NTU = UA / Cmin = 0,973
- Cmin / Cmax = 0,500

Equations:

- $\Delta T_{lm} = \Delta T_{lm,PF}$ for Parallel-flow Hxs
- $\Delta T_{lm} = \Delta T_{lm,CF}$ for Counterflow Hxs
- $\Delta T_{lm} = \Delta T_{lm,CF}$ for Shell-and-Tube Hxs
- $q = UA\Delta T_{lm}$
- $q = C_S \times \text{abs}(T_{S,i} - T_{S,o})$
- $q = C_T \times \text{abs}(T_{T,o} - T_{T,i})$
- Temperature ratios for correction factor (F) evaluation - only useful for shell-and-tube HX since, $\Delta T_{lm} = F\Delta T_{lm,CF}$
- $R = \frac{T_{S,i} - T_{S,o}}{T_{T,o} - T_{T,i}}$
- $P = \frac{T_{T,o} - T_{T,i}}{T_{S,i} - T_{T,i}}$
- $\epsilon = \frac{q}{q_{max}}$
- $NTU = \frac{UA}{C_{min}}$
- $C_r = \frac{C_{min}}{C_{max}}$ (Heat capacity ratio)

Exploring the Software - Design Problem (1/4)

A heat exchanger is to be designed to cool ethyl alcohol solution from 75°C ($T_{h,i}$) to 45°C ($T_{h,o}$) with cooling water entering the tube side at 15°C ($T_{c,i}$). The heat capacity rates ($C = \dot{m}.c_p$) for the hot fluid and cold fluid are 30 kW.K^{-1} and 40 kW.K^{-1} , respectively. Consider that the overall heat transfer coefficient (U) based on the outer tube surface is equal to $500 \text{ W.m}^{-2}.\text{C}^{-1}$.

Determine the total heat transfer surface area required for each HX type:

- Parallel-flow heat exchanger;
- Counterflow heat exchanger;
- shell-and-tube heat exchanger with three shell passes and six tube passes.

Exploring the Software - Design Problem (2/4)

- Parallel-flow HX

Temperature Distributions

Temp vs Distance (0.0 to 1.0). Shell (red line) and Tube (blue line) temperatures are shown.

Heat Capacity Rates:

Shell = 30.0 * Hot
Tube = 40.0 * Cold

Calculation Method:

Design (LMTD)
 Performance (Effectiveness-NTU)

Desired Shell Outlet Temp: 45

Configuration:

Parallel Flow
Modify

Temperature Option:

Dimensional
 NonDim

Design Data:

Overall HT Coeff x Area (UA) = 35,63 *
Log-Mean Temp Diff (LMTD) = 25,247
Q based on LMTD = 899,64 *
Q based on Shell Fluid T-Diff = 900,00 *
Q based on Tube Fluid T-Diff = 900,00 *
R = (T_{Sin}-T_{Sout}) / (T_{Tout}-T_{Tin}) = 0,000
P = (T_{Tout}-T_{Tin}) / (T_{Sin}-T_{Tin}) = 0,014

Temperature Data:

Shell In = 75 Tube In = 15
Shell Out = 45,000 Tube Out = 37,500

Performance Data:

Effectiveness = Q / Q_{max} = 0,500
NTU = UA / C_{min} = 1,188
C_{min} / C_{max} = 0,750

Student: _____

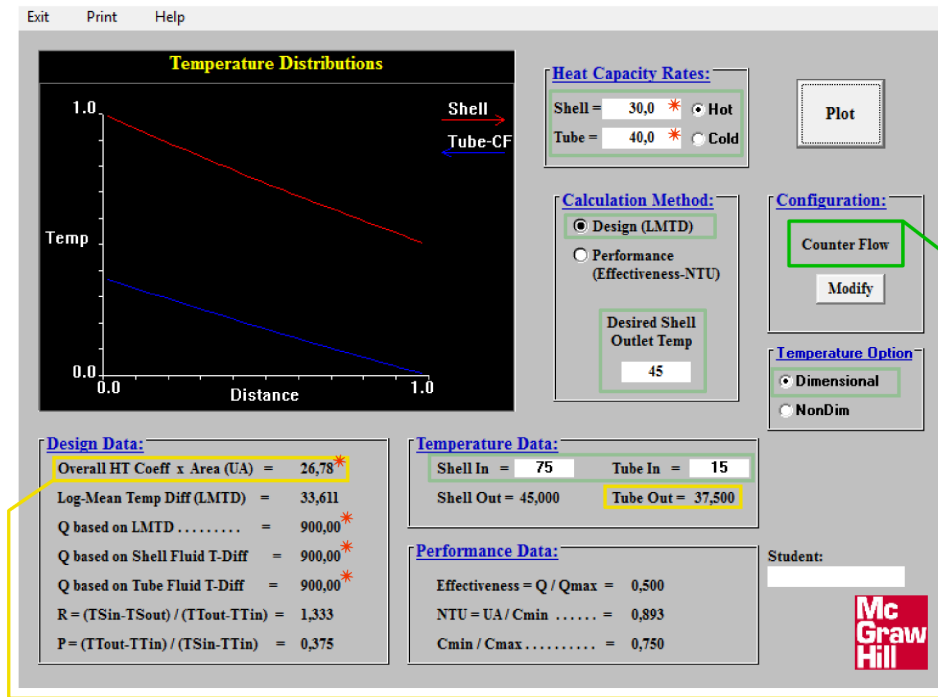
Mc Graw Hill

Annotations:

- Green box: Input Data
- Yellow box: Relevant Output Data
- Note: "Modify" >> "Concentric Tube" >> "New Setup" >> "Parallel Flow" >> "Nodes=30" >> "Update" >> "Return"
- Equation: $UA = 35.63 \text{ kW.K}^{-1} \Rightarrow A = 71.26 \text{ m}^2$
- Footnote: * When the heat capacity rates are specified in kW.K^{-1} UA is given in kW.K^{-1} and the rates of heat transfer in kW.

Exploring the Software - Design Problem (3/4)

(b) Counterflow HX



Input Data

Relevant Output Data

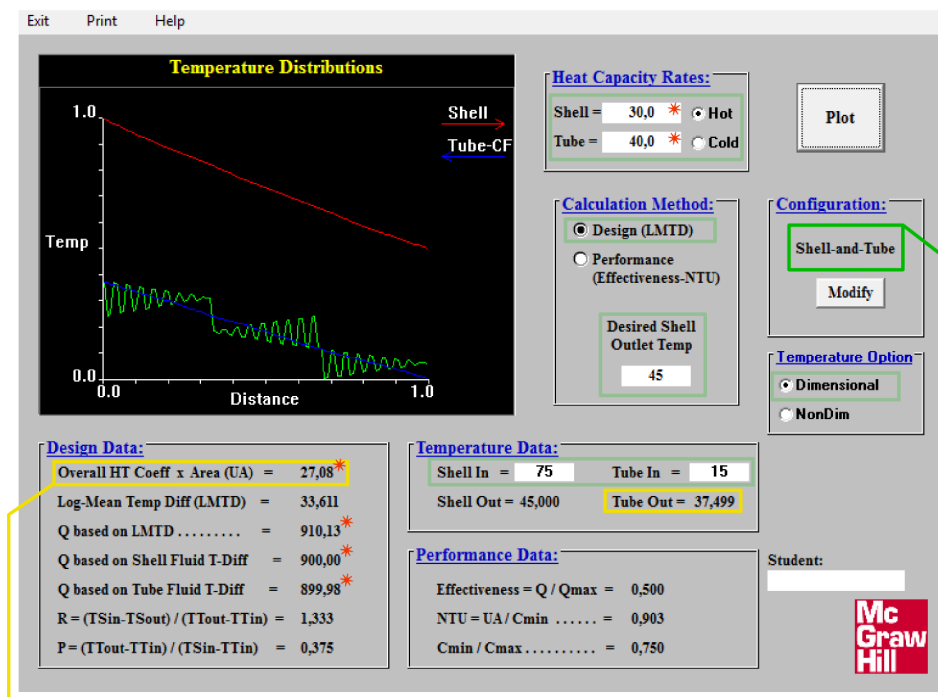
"Modify">>"Concentric Tube">>
 "New Setup">>"Counter Flow">>
 "Nodes=30">>"Update">>"Return"

$$UA = 26.78 \text{ kW.K}^{-1} \Rightarrow A = 53.56 \text{ m}^2$$

* When the heat capacity rates are specified in kW.K⁻¹ UA is given in kW.K⁻¹ and the rates of heat transfer in kW.

Exploring the Software - Design Problem (4/4)

(c) Shell-and-tube HX with 3 shell passes and 6 tube passes



Input Data

Relevant Output Data

"Modify">>"Shell-and-Tube">>
 "New Setup">>"Shell Passes=3">>
 "Baffles=16">>"Update">>"Return"

$$UA = 27.08 \text{ kW.K}^{-1} \Rightarrow A = 54.16 \text{ m}^2$$

* When the heat capacity rates are specified in kW.K⁻¹ UA is given in kW.K⁻¹ and the rates of heat transfer in kW.

Exploring the Software - Performance Calculation (1/4)

A shell-and-tube HX with **two shell passes and four tube passes** is cooling $1.5 \text{ kg}\cdot\text{s}^{-1}$ of oil initially at 90°C with water entering at 19°C with a mass flow rate of $1.0 \text{ kg}\cdot\text{s}^{-1}$. Consider $UA = 6300 \text{ W}\cdot\text{K}^{-1}$, $c_{p,h} = 2100 \text{ J}\cdot\text{K}^{-1}\cdot\text{kg}^{-1}$ and $c_{p,c} = 4180 \text{ J}\cdot\text{K}^{-1}\cdot\text{kg}^{-1}$. Determine the heat transfer rate and the outlet oil and water temperatures. The heat capacity rates of the hot and cold fluid streams, C_h and C_c , respectively are:

$$C_h = \dot{m}_h c_{p,h} = 1.5 \times 2100 = 3150 \text{ W}\cdot\text{K}^{-1}$$

$$C_c = \dot{m}_c c_{p,c} = 1.0 \times 4180 = 4180 \text{ W}\cdot\text{K}^{-1}$$

Exploring the Software - Performance Calculation (2/4)

The screenshot shows the software interface with the following data and annotations:

- Temperature Distributions:** A plot of Temperature vs. Distance (0.0 to 1.0). The Shell temperature (red line) decreases from 90°C to approximately 40.9°C. The Tube temperature (blue line) increases from 19°C to approximately 55.9°C. The plot shows a sawtooth pattern for the tube temperature due to multiple passes.
- Heat Capacity Rates:**
 - Shell = 3.150,0 * (Hot)
 - Tube = 4.180,0 * (Cold)
- Calculation Method:** Performance (Effectiveness-NTU)
- Configuration:** Shell-and-Tube
- Temperature Option:** Dimensional
- Overall HT Coeff x Area (UA):** 6300 *
- Design Data:**
 - Overall HT Coeff x Area (UA) = 6.300,00 *
 - Log-Mean Temp Diff (LMTD) = 27,537
 - Q based on LMTD = 173.481,20 *
 - Q based on Shell Fluid T-Diff = 154.563,40 *
 - Q based on Tube Fluid T-Diff = 154.563,40 *
 - R = (T_{Sin}-T_{Sout}) / (T_{Tout}-T_{Tin}) = 1,327
 - P = (T_{Tout}-T_{Tin}) / (T_{Sin}-T_{Tin}) = 0,521
- Temperature Data:**
 - Shell In = 90, Tube In = 19
 - Shell Out = 40,932, Tube Out = 55,977
- Performance Data:**
 - Effectiveness = Q / Q_{max} = 0,691
 - NTU = UA / C_{min} = 2,000
 - C_{min} / C_{max} = 0,754

Annotations and results:

- Green box: Input Data
- Yellow box: Relevant Output Data
- Green arrow: "Modify" >> "Shell-and-Tube" >> "New Setup" >> "Shell Passes=2" >> "Baffles=16" >> "Update" >> "Return"
- Results:
 - $T_{oil,out} = 40.932^\circ\text{C}$
 - $T_{water,out} = 55.977^\circ\text{C}$
 - $q \approx 154.6 \text{ kW}$
- * When the heat capacity rates are specified in $\text{W}\cdot\text{K}^{-1}$ UA needs to be specified also in $\text{W}\cdot\text{K}^{-1}$ and the rates of heat transfer are given in W.

Exploring the Software - Performance Calculation (3/4)

Temperature Distributions

Temp vs Distance (0.0 to 1.0)

Heat Capacity Rates:
 Shell = 3.150 * Hot
 Tube = 4.180 * Cold

Calculation Method:
 Design (LMTD)
 Performance (Effectiveness-NTU)

Configuration:
 Shell-and-Tube
 Modify

Temperature Option:
 Dimensional
 NonDim

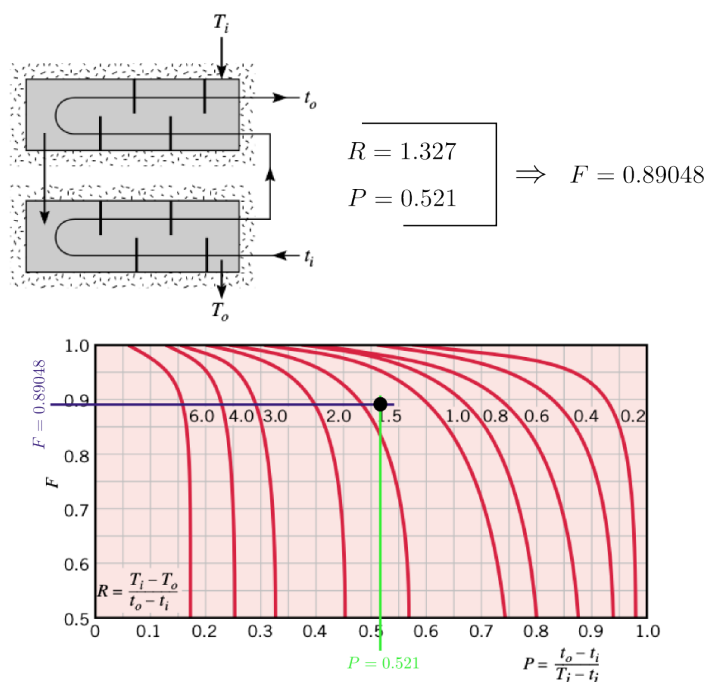
Design Data:
 Overall HT Coeff x Area (UA) = 6.300,00
 Log-Mean Temp Diff (LMTD) = 27,537
 Q based on LMTD = 173.481,20
 Q based on Shell Fluid T-Diff = 154.563,40
 Q based on Tube Fluid T-Diff = 154.563,40
 R = (T_{Sin}-T_{Sout}) / (T_{Tout}-T_{Tin}) = 1,327
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Temperature Data:
 Shell In = 90 Tube In = 19
 Shell Out = 40,932 Tube Out = 55,977

Performance Data:
 Effectiveness = Q / Q_{max} = 0,691
 NTU = UA / C_{min} = 2,000
 C_{min} / C_{max} = 0,754

Annotations:
 R = 1.327
 P = 0.521
 F = 0.89048
 ΔT_{lm,c} = FΔT_{lm,CF} = 24.52 °C
 q_{lm,c} = UAΔT_{lm,c} = Fq_{lm} ≈ 154.5 kW
 * When the heat capacity rates are specified in W.K⁻¹ UA needs to be specified also in W.K⁻¹ and the rates of heat transfer are given in W.

Exploring the Software - Performance Calculation (4/4)



Useful Relations

1. Overall Energy Balance:

- Hot Fluid
 $q = C_h (T_{h,i} - T_{h,o})$
- Cold Fluid
 $q = C_c (T_{c,o} - T_{c,i})$

2. Log Mean Temperature Difference (LMTD) Method:

- $q = UA\Delta T_{lm}$
- For Multipass and cross-flow HXs

$$\Delta T_{lm,c} = F \Delta T_{lm,CF}$$
$$\Rightarrow F = \frac{q}{q_{lm}}$$

3. Effectiveness-NTU Method:

$$\varepsilon = \frac{q}{q_{\max}}$$

$$q_{\max} = C_{\min} (T_{h,i} - T_{c,i})$$

$$C_{\min} = \text{Min} (C_c, C_h)$$

$$NTU = \frac{UA}{C_{\min}}$$

$$\varepsilon = f(NTU, C_r)$$

$$NTU = f(\varepsilon, C_r)$$

- $C_r = C_{\min}/C_{\max}$ - Heat capacity ratio
- $C = \dot{m}.c_p$ - Heat capacity rate