

Active Graphene Plasmonics with a Drift-Current Bias

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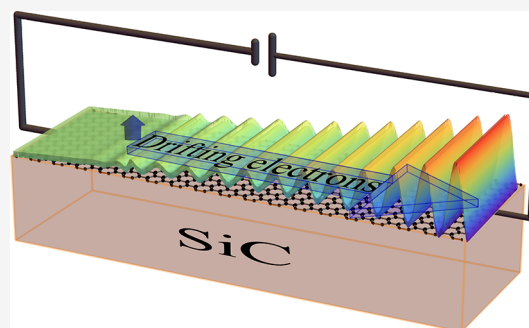
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Supporting Information

ABSTRACT: We theoretically demonstrate that a system formed by a drift-current biased graphene sheet on a silicon carbide substrate enables loss compensation and plasmon amplification. The active response of the graphene sheet is rooted in the optical pumping of the graphene plasmons with the gain provided by the streaming current carriers. The proposed system behaves as an optical amplifier for the plasmons copropagating with the drifting electrons and as a strong attenuator for the counter-propagating plasmons. Furthermore, we show that the feedback obtained by connecting the input and output of the system, for example, as a ring-shaped graphene–silicon carbide nanoresonator, combined with the optical gain provided by the drifting electrons, may lead to spasing.

KEYWORDS: graphene, plasmonics, nonreciprocity, active medium



INTRODUCTION

The unprecedented field enhancement and subwavelength confinement provided by surface plasmon polaritons (SPPs),¹ charge density waves supported by metal-type surfaces, have pushed the field of plasmonics^{2–4} to the frontline of scientific research. The unique features of the SPPs opened the door to a plethora of new phenomena and important applications, such as in nanophotonic circuitry,^{5,6} photonic metamaterials,⁷ solar energy harvesting,⁸ superlensing,^{9,10} chemical and medical sensing,^{11–13} and photothermal cancer therapy.^{14,15}

With the isolation of graphene¹⁶ and the discovery of its remarkable electronic and optical properties,^{17,18} the field of plasmonics experienced a new boost.^{19–24} Much of the interest in graphene plasmonics comes from the fact that the optical properties of this one-atom thick material are highly tunable by means of chemical doping or electrostatic gating, offering a unique opportunity to dynamically manipulate the SPPs properties.

Unfortunately, the high absorption (or ohmic) losses that intrinsically characterize plasmonic materials, such as metals and semiconductors, caused by different scattering mechanisms (e.g., electron–phonon and electron–electron scattering) and by Landau damping^{25,26} impose harsh limitations in many nanophotonic applications. For instance, the ohmic losses in silver may limit the SPP propagation length to about 20 nm at near-UV frequencies where the field confinement is strongest.²⁷ The propagation length increases to values up to 20 μm for visible frequencies but at the expense of poor wave localization.^{1,27} The plasmonic dissipation in graphene is also quite significant,^{28–31} restricting the SPP propagation length to 1 μm at mid-infrared frequencies and room temperature, and 46 to about 10 μm at cryogenic temperatures.³²

Even though the development of new plasmonic materials^{33–35} may help mitigate the detrimental effects of ohmic losses, the ultimate limits imposed by plasmonic absorption (e.g., in the SPP propagation length or even in the resolution of superlenses) can be only surpassed by introducing optical gain into the systems. In this context, several theoretical and experimental studies on plasmonic loss compensation and SPP amplification have been reported.^{27,36–54} In particular, the amplification of long-range SPPs was experimentally demonstrated in systems formed by gold nanofilms combined with optically pumped gain media such as dye solutions⁴⁷ and fluorescent polymers.⁴⁸ Moreover, merging the SPP amplification with some feedback mechanism may lead to the spontaneous generation of SPPs, an effect known as spasing or plasmonic lasing.^{55–65}

In this work, we theoretically predict the full compensation of plasmonic loss and the amplification of SPPs in a nanostructure formed by a drift-current biased graphene sheet deposited on a silicon carbide (SiC) substrate [see Figure 1]. The graphene–SiC plasmons gain energy from the electrons drifting on the graphene sheet, a process known as “negative Landau damping”.⁶⁶ It is shown that the considered graphene–SiC nanostructure acts as an amplifier for the SPPs copropagating with the drifting electrons and as a very effective attenuator for the counter-propagating plasmons. Moreover, 71

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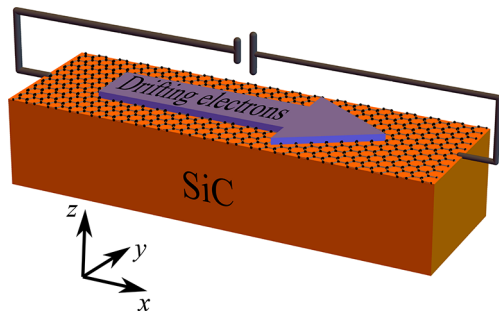


Figure 1. Drift-current biased graphene sheet on a SiC substrate. A graphene sheet deposited on the top of a SiC substrate is biased with a drift-electric current due to a static voltage generator.

we demonstrate that by connecting the input and the output of the system, for example, with a ring-shaped graphene–SiC nanostructure, it may be possible to spontaneously generate graphene SPPs (spacing^{55–65}). It should be mentioned that the SPP amplification by means of a drift current biasing was studied in refs 67 and 68 in a related system but with the effect of the drift current bias on the SPP waves treated simply by adapting classical formulas from microwave theory to the graphene.

RESULTS AND DISCUSSION

Figure 1 presents a schematic illustration of the structure under study. It consists of a graphene sheet biased with a drift electric current deposited on the top of a SiC substrate. We assume that the region above graphene is air. The frequency dispersion and dissipation in SiC are modeled by the dielectric function reported in refs 24 and 69. As long as $k_B T \ll \mu_c$ (where k_B is the Boltzmann's constant, T is the temperature, and μ_c is the chemical potential), the graphene sheet response (without drifting electrons) may be characterized by the “low-temperature” nonlocal random-phase approximation (RPA) surface conductivity $\sigma_g(\omega, q)$ ($q = \sqrt{k_x^2 + k_y^2}$ is the in-plane wavenumber) reported in ref 21, which includes both the intraband and interband contributions. For ω and q complex, we evaluate $\sigma_g(\omega, q)$ using the analytical continuation formulas reported in ref 70. The loss due to electronic scattering is modeled using the relaxation-time approximation.⁷¹ We assume throughout

this article that the relaxation time in graphene is $\tau = 170$ fs,^{72,73} which is a conservative value compared to more recent observations.³² Moreover, in the main text the chemical potential of the graphene sheet is taken equal to $\mu_c = 0.35$ eV. For this chemical potential, the low-temperature limit $k_B T \ll \mu_c$ is satisfied for temperatures up to 400 K. The space-time variation is assumed to be of the form $e^{ik_x x} e^{-i\omega t}$.

The graphene conductivity in the presence of a drift-current bias may be obtained from the conductivity without drift using a Galilean-Doppler shift^{66,74}

$$\sigma_g^{\text{drift}}(\omega, k_x) \approx (\omega/\tilde{\omega})\sigma_g(\tilde{\omega}, q)|_{q=\sqrt{k_x^2}} \quad (1)$$

where $\tilde{\omega} = \omega - k_x v_0$ is the Doppler-shifted frequency and k_x is the wavenumber along the x -direction. Here, $\sigma_g(\omega, q)$ is the nonlocal no-drift graphene conductivity discussed in the previous paragraph. It is assumed that the drifting electrons flow along the x -direction with drift velocity v_0 [see Figure 1] and that the in-plane electric field is oriented along x (longitudinal excitation). The drift velocity is typically some fraction of the Fermi velocity v_F . Remarkably, for sufficiently large positive v_0 and k_x , ω and $\tilde{\omega}$ have different signs, and consequently $\text{Re}\{\sigma_g^{\text{drift}}(\omega, k_x)\}$ may become negative in the upper-half frequency plane. Thereby, the drifting electrons may turn the graphene sheet into an active medium with optical gain⁶⁶ [see Figure 2]. The impact of collisions (scattering loss) on $\text{Re}\{\sigma_g^{\text{drift}}(\omega, k_x)\}$ is further discussed in the Supporting Information. In Figure 2, \hbar is the reduced Planck constant and $k_F = \mu_c/(\hbar v_F)$ is the Fermi wavenumber.

Before discussing the loss compensation and plasmon amplification in the graphene–SiC waveguide, it is instructive to first examine the scattering properties of the drift-current biased graphene sheet when it is deposited on the top of a dielectric slab. To this end, we consider that a transverse magnetic (TM) wave with magnetic field directed along y [see the inset of Figure 3] and characterized by the wavenumber k_x illuminates the graphene sheet. The complex amplitude of the incident magnetic field is denoted by H_y^{inc} and the (real-valued) oscillation frequency by ω .

Because of the intrinsic material absorption, the superposition of the incident and reflected evanescent waves typically gives rise to a power flux toward the graphene

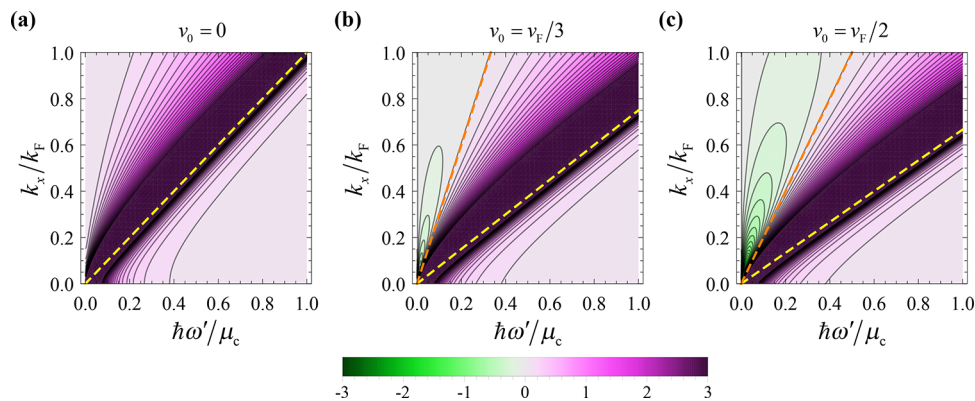


Figure 2. Graphene conductivity. Real part of the graphene conductivity in the upper-half frequency-plane as a function of the normalized frequency $\hbar\omega'/\mu_c$ ($\omega = \omega' + i\omega''$ with $\hbar\omega''/\mu_c = 0.001$) and wavenumber k_x/k_F for different drift velocities v_0 . The conductivity normalization factor in the contour plots is $\sigma_0 = e^2/(4\hbar)$, with e the electron charge. The yellow dashed line corresponds to the square-root singularity of the graphene conductivity that occurs at $\omega' \approx k'_x(v_F + v_0)$.⁷⁰ The orange dashed lines in (b,c) correspond to $\omega' = k'_x v_0$. The negative Landau damping emerges in the region $\omega' < k'_x v_0$ (region on the left-hand side of the orange line).

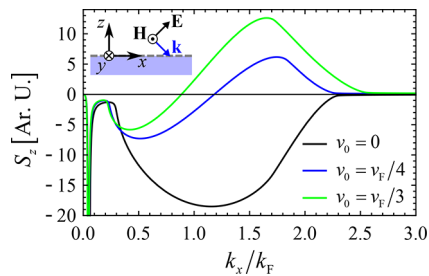


Figure 3. Poynting vector for plane wave incidence. Poynting vector (component perpendicular to the interface in arbitrary units) as a function of k_x for different drift velocities at $f = 25$ THz. The inset depicts a TM plane wave illuminating the drift-current biased graphene sheet on a dielectric substrate with relative permittivity $\epsilon_{r,d} = 4$.

curve in Figure 3). In contrast, with the drift-current biasing and for a large k_x (blue and green curves in Figure 3), the energy density flux S_z may flip its sign so that the graphene sheet may generate energy that flows away from it. This gain regime stems from the negative Landau damping effect reported in ref 66 which enables the transfer of kinetic energy from the drifting electrons to the radiation field.

To study the opportunities created by the negative Landau damping effect, next we characterize the SPPs supported by the graphene–SiC system illustrated in Figure 1. The dispersion characteristic of the SPPs is given by²⁴

$$\frac{1}{\gamma_0} + \frac{\epsilon_{r,\text{SiC}}(\omega)}{\gamma_{\text{SiC}}} - \frac{\sigma_g^{\text{drift}}}{i\omega\epsilon_0} = 0 \quad (3)$$

where $\epsilon_{r,\text{SiC}}(\omega)$ is the SiC dielectric function^{24,69} and $\gamma_{\text{SiC}} = \sqrt{k_x^2 - \epsilon_{r,\text{SiC}}(\omega/c)^2}$ is the attenuation constant (along z) of the plasmons in the SiC slab. If the drift velocity is set identical to zero ($\sigma_g^{\text{drift}} \rightarrow \sigma_g$), one recovers the well-known dispersion equation for the plasmons supported by the graphene–SiC system.

Figure 4 depicts the dispersion characteristic of the SPPs supported by the structure for different drift velocities v_0 . The dispersion is found by solving eq 3 with respect to $k_x = k'_x + ik''_x$ for real-valued ω . For low-frequencies, the SiC behaves as a dielectric with positive permittivity. This happens for ω below the SiC resonance frequency $\omega_{\text{TO}}/(2\pi) = 22.78$ THz (ω_{TO} is the bulk transverse optical (TO) phonon frequency).^{24,69} In such a regime, the system is analogous to a graphene sheet placed on the top of a dielectric substrate, similar to the systems analyzed by us in refs 70 and 75. As shown in previous works,^{70,75–80} the drift-current biasing causes a symmetry

sheet. The z -component of the total Poynting vector in the air region is given by $S_z = \frac{E_y^{\text{inc}}}{2\omega\epsilon_0} \text{Im}\{\gamma_0(1-R)(1+R)^*\}$. Here,

$$R(\omega, k_x) = \frac{\gamma_0\gamma_d + \kappa_g^{\text{drift}}(\gamma_d - \gamma_0\epsilon_{r,d})}{\gamma_0\gamma_d - \kappa_g^{\text{drift}}(\gamma_d + \gamma_0\epsilon_{r,d})} \quad (2)$$

is the magnetic field reflection coefficient,⁷⁵ $\kappa_g^{\text{drift}} = i\omega\epsilon_0/\sigma_g^{\text{drift}}$, ϵ_0 is the free-space permittivity, $\gamma_0 = \sqrt{k_x^2 - (\omega/c)^2}$ and $\gamma_d = \sqrt{k_x^2 - \epsilon_{r,d}(\omega/c)^2}$ are the attenuation constants (along z) in the air and dielectric regions, respectively, c is the speed of light in vacuum, and the “*” symbol denotes complex conjugation. Evidently, in the absence of a drift-current biasing the z -component of the Poynting vector is negative ($S_z < 0$) and thereby the graphene sheet absorbs energy (see the black

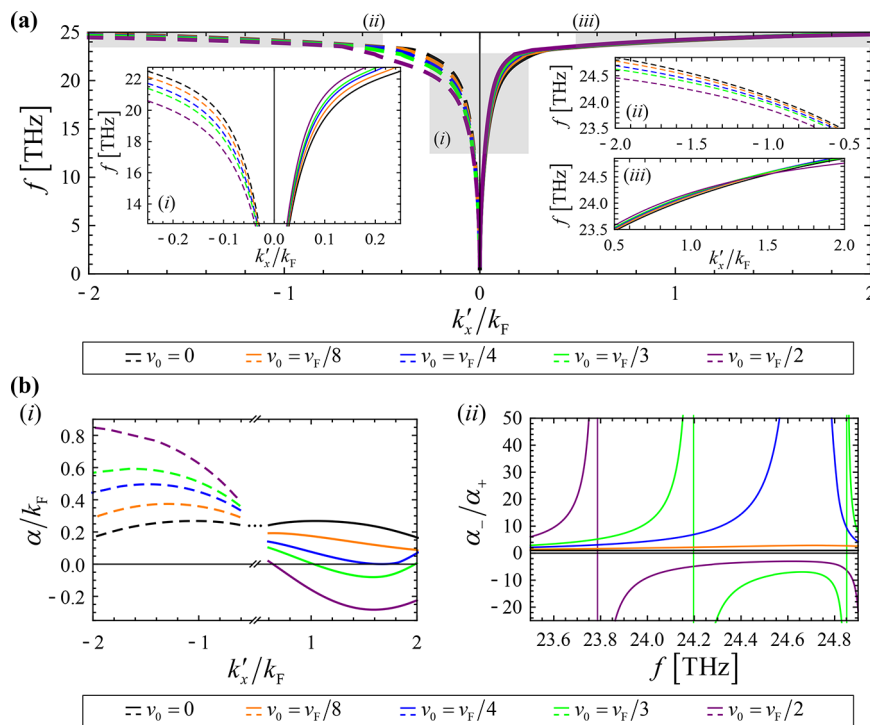


Figure 4. SPPs dispersion diagrams. (a) Main panel: Frequency dispersion of the SPPs supported by the graphene–SiC system as a function of the real part of the SPP wavenumber for several drift velocities v_0 ; (i), (ii), and (iii) zoom-in views of the shaded rectangular areas of the main panel. (b) (i) SPP attenuation constant ($\alpha = k''_x \text{sgn}(k'_x)$) as a function of the real part of the SPP wavenumber. (ii) Ratio between the attenuation constants of the SPPs that propagate along the $-x$ and $+x$ direction as a function of the frequency.

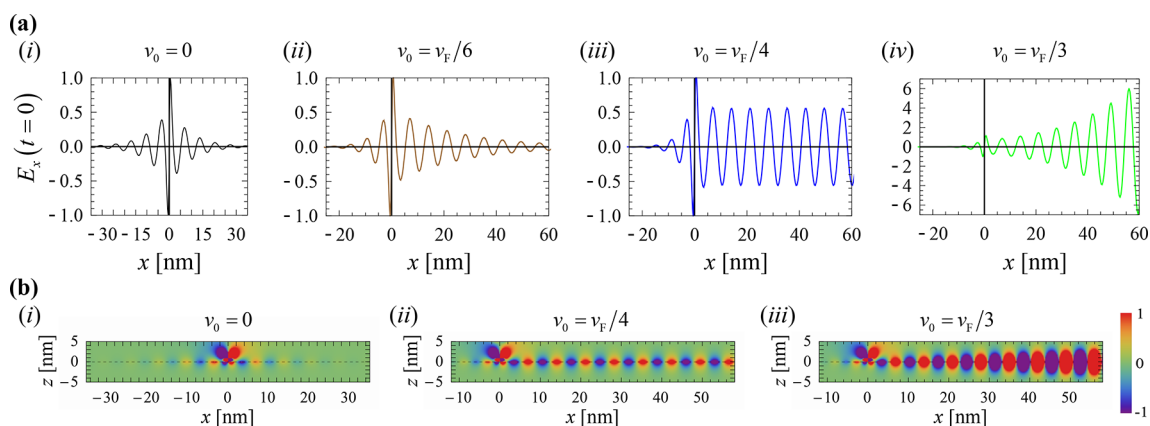


Figure 5. SPP excitation by a near-field emitter. (a) Time snapshots of the x -component of the electric field E_x (in arbitrary unities) as a function of x and for $z = 0$, for several drift velocities v_0 . (b) Time snapshots of the x -component of the electric field E_x as a function of x and z and for several drift velocities v_0 . The frequency of operation is $\omega/(2\pi) = 24.7$ THz and the emitter is positioned at the point $(x, z) = (0, 1$ nm). The drift velocity v_0 is indicated at the top of each panel.

178 breaking in the SPPs dispersion such that $\omega(k'_x) \neq \omega(-k'_x)$ [see
179 inset (i) of Figure 4a]. Similar nonreciprocal effects may also
180 occur in systems with moving components.^{81–83} Clearly, the
181 degree of asymmetry increases with the drift velocity v_0 , and for
182 sufficiently large v_0 it gives rise to regimes of unidirectional
183 propagation wherein the SPPs are allowed to propagate only
184 along the $+x$ direction (the direction of the drifting
185 electrons).^{70,75}

186 On the other hand, for frequencies above the resonance and
187 below 27.82 THz, the real part of the SiC permittivity is
188 negative ($\text{Re}\{\epsilon_{\text{SiC}}\} < 0$) and thereby SiC has a plasmonic
189 (metal-type) response.^{24,69} In this article, we focus on the
190 spectral range [22.78–27.82 THz] wherein $\text{Re}\{\epsilon_{\text{SiC}}(\omega)\} < 0$.
191 In this range, the system supports plasmons with very short
192 wavelengths, which are essential to access the optical gain
193 regime with $\text{Re}\{\sigma_{\text{g}}^{\text{drift}}\} < 0$ characterized by $\omega - k'_x v_0 < 0$.

194 The metal-phase of SiC, when $\text{Re}\{\epsilon_{\text{SiC}}\} < 0$, leads to a
195 pronounced spectral asymmetry of the graphene plasmons
196 dispersion such that $\omega(k'_x) \neq \omega(-k'_x)$ [see Figure 4a, especially
197 the insets (ii) and (iii)]. Even more interesting, Figure 4b(i),
198 (ii) show that with the drift-current bias, the attenuation
199 constant $\alpha = k''_x \text{sgn}(k'_x)$ of the SPPs copropagating (counter-
200 propagating) with the drifting electrons is greatly reduced
201 (enhanced). Crucially, for large enough drift velocities v_0 , the
202 attenuation constant of the SPPs copropagating with the
203 drifting electrons ($k'_x > 0$) vanishes or even becomes negative.
204 Specifically, Figure 4b(i) shows that the graphene plasmons
205 attenuation can be fully suppressed (that is, $\alpha = 0$) for drift
206 velocities on the order of $v_0 = v_F/4$ [see blue solid curve], and
207 for $v_0 > v_F/4$ it can be even overcompensated (that is, $\alpha < 0$)
208 [see green and purple solid curves]. Therefore, these results
209 indicate that for $v_0 \geq v_F/4$, the graphene–SiC system may be
210 either immune to attenuation or behave as an optical amplifier
211 for the graphene plasmons copropagating with the drifting
212 electrons. In contrast, for counter-propagating plasmons ($k'_x <$
213 0), α increases with the drift velocity v_0 [see dashed curves in
214 Figure 4b(i)], and hence, the drift current strongly suppresses
215 the counter-propagating plasmons.

216 The SPP amplification strength and bandwidth increase with
217 the drift velocity v_0 . Curiously, the amplification strength $-\alpha$
218 for $v_0 = v_F/2$ may be comparable or even larger than the
219 attenuation factor α of the SPPs without the drift-current
220 biasing [see purple solid and black curves in Figure 4b(i)].

Furthermore, the attenuation strength along the $-x$ direction
221 for $v_0 = v_F/2$ is about 4 times larger than without a drift current
222 [see purple and black dashed curves in Figure 4b(i)]. On the
223 other hand, Figure 4b(ii) shows that the bandwidth of the SPP
224 amplification regime (range of frequencies where $\alpha_+ < 0$) is
225 about 0.6 THz for $v_0 = v_F/3$ [see green curve], increasing up to
226 around 1.2 THz as the drift velocity approaches $v_0 = v_F/2$ [see
227 purple curve]. Interestingly, it is shown in the Supporting
228 Information that by increasing the chemical potential μ_c of
229 graphene, one can boost the amplification bandwidth and the
230 amplification gain $-\alpha$, and thereby reduce the threshold
231 velocity v_0 at which the attenuation is fully suppressed ($\alpha = 0$).
232 This happens because a larger μ_c implies a larger k'_x (that is, the
233 SPPs are more confined), allowing that $\tilde{\omega}$, and consequently
234 $\text{Re}\{\sigma_{\text{g}}^{\text{drift}}(\omega, k_x)\}$, become negative for lower drift velocities. For
235 $v_0 = v_F/2$, our system enables gain bandwidths of about 5% for
236 $\mu_c = 0.35$ eV, increasing to 6% for $\mu_c = 0.5$ eV (see the
237 Supporting Information).
238

To further highlight the consequences of the loss
239 compensation and gain regimes in the graphene–SiC system,
240 next we consider the scenario wherein a linearly polarized
241 emitter (a short vertical electric dipole) placed in the vicinity
242 of the graphene sheet is used to excite the graphene plasmons.
243 The radiated and scattered fields are obtained from a
244 Sommerfeld-type integral (an inverse Fourier-Laplace trans-
245 form in k_x) as described in the Supporting Information.
246 Because of the active response of the system, when $v_0 > 0$ the
247 integral in k_x must be calculated along a line in the lower half
248 k_x -plane parallel to the real- k_x axis. The integration path must
249 be below all poles (for details see the Supporting Information).
250

Figure 5 shows the time snapshots of the x -component of
251 the electric field for a graphene sheet biased with different drift
252 velocities v_0 . As expected, without a drift-current biasing ($v_0 =$
253 0) the two identical counter-propagating SPPs excited by the
254 near-field emitter are equally attenuated as they propagate
255 along the graphene–SiC interface [see Figures 5a,b(i)]. In
256 such circumstances, the SPP field attenuation is simply
257 determined by the graphene and SiC damping rates. Quite
258 differently, when a drift-current biasing is applied ($v_0 \neq 0$), the
259 plasmons copropagating with the drifting electrons (the $+x$
260 direction) are significantly less attenuated than the plasmons
261 propagating in the opposite direction (the $-x$ direction) [see
262 Figure 5a(ii)]. In particular, for $v_0 = v_F/4$ the system supports 263

264 loss-free plasmons that propagate along the $+x$ direction [see
265 Figure 5a(iii) and Figure 5b(ii)], which is consistent with the
266 attenuation suppression predicted in Figure 4b(i),(ii). Notably,
267 for drift velocities $v_0 > v_F/4$ the plasmons copropagating with
268 the drifting electrons (the $+x$ direction) are amplified, whereas
269 the plasmons propagating along the opposite direction are
270 strongly attenuated [see Figure 5a(iv) and Figure 5b(iii)], as
271 expected from the results of Figure 4b(i),(ii). As previously
272 discussed, the optical gain is due to the conversion of kinetic
273 energy of the drifting electrons into plasmon oscillations.⁶⁶ In
274 the Supporting Information, we show that by increasing the
275 chemical potential μ_c , it is possible to reach regimes of lossless
276 propagation and plasmon amplification for drift velocities even
277 lower than $v_F/4$.

278 So far, it was assumed that the graphene–SiC guide has
279 infinite length in the longitudinal direction (x -direction). Let
280 us now consider finite-length nanostructures. In particular, let
281 us consider a “circular” graphene resonator formed by a ring-
282 shaped graphene ribbon with a drift-current bias placed on the
283 top of a SiC substrate, as sketched in Figure 6a. The modes
284 supported by such a ring-shaped graphene resonator can be
285 found enforcing periodic boundary conditions. Specifically, if

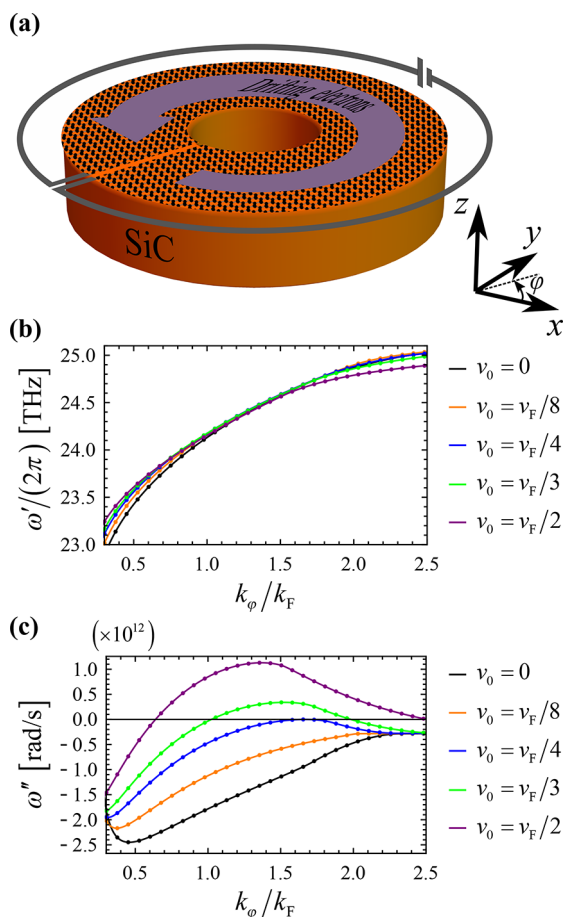


Figure 6. Ring-shaped graphene–SiC nanoresonator. (a) Circular graphene nanoresonator formed by a ring-shaped graphene ribbon biased with a drift current. (b) Real and (c) imaginary parts of the oscillation frequencies of the natural modes as a function of k_ϕ for different drift velocities v_0 . Discrete points: oscillation frequencies for a circular graphene nanoresonator with radius $R = 25$ nm. Solid lines: oscillation frequencies for a circular resonator with $R \rightarrow \infty$. The spasing occurs for modes with $\omega'' > 0$.

the perimeter of the resonator is L then the allowed wave 286 numbers are $k_\phi = 2\pi n/L$, that is, the wavenumber is necessarily 287 real-valued. Thus, the natural modes of a circular resonator can 288 be found by looking for complex-valued solutions $\omega = \omega(k_\phi)$ 289 of eq 3 with $k_\phi = 2\pi n/L$ real-valued. The time variation is $e^{-i\omega t}$ 290 $= e^{-i\omega' t} e^{\omega'' t}$ with $\omega = \omega' + i\omega''$ as the complex resonance 291 frequency of the relevant mode. The system will be unstable if 292 $\omega'' > 0$. Here, we neglect the curvature of the circular 293 resonator, so that $\omega = \omega(k_\phi)$ may be determined from the 294 modal dispersion [eq 3] of the associated planar geometry. 295 Furthermore, the effect of the finite lateral width of the 296 graphene ribbon is disregarded in our analysis. Using these 297 approximations, we depict in Figure 6b,c the real and 298 imaginary parts of the oscillation frequency (ω) as a function 299 of the normalized k_ϕ for different drift velocities v_0 . 300 Remarkably, Figure 6c shows that for $v_0 > v_F/4$ the nanoring 301 resonator supports oscillations that grow exponentially with 302 time ($\omega'' > 0$). The wave instabilities stem from the feedback 303 that is obtained by connecting the input and output of the 304 optical amplifier. As expected, the growth rate increases as the 305 drift velocity v_0 increases, and for $v_0 = v_F/2$ the growth rate 306 (that is, the magnitude of ω'') can be as high as $\omega'' \approx 1.13 \times$ 307 10^{12} s^{-1} . The emission rate of the plasmons is determined by 308 ω'' . In the example of Figure 6c, before the saturation is 309 reached, the energy in the resonator will grow by a factor of e 310 ≈ 2.7 every $\frac{1}{2\pi} \left| \frac{\omega'}{\omega''} \right| \approx 10.8$ periods of oscillation. Therefore,

the graphene nanoresonator may be regarded as spaser 312 pumped by drifting electrons.^{55–65} 313 In the Supporting Information, it is shown that the 314 relativistic Doppler-shift model for the graphene conductivity^{76–78,84,85} 315 leads to qualitatively similar wave instabilities but 316 with a slightly larger growth rate. In our understanding, the 317 Galilean–Doppler shift theory is the most accurate model 318 when the electron–electron interactions predominate and 319 force the electrons to move with constant velocity v_0 .⁷⁴ In 320 addition, in the Supporting Information it is shown that the 321 wave instabilities are rooted in the intraband light-matter 322 interactions. 323

CONCLUSIONS

In summary, we have demonstrated that a system formed by a 325 drift-current biased graphene sheet deposited on a SiC 326 substrate may enable the full compensation of plasmonic 327 losses and the amplification of graphene plasmons. The 328 plasmonic gain is due to the conversion of the kinetic energy 329 of the moving electrons into short-wavelength plasmons. It was 330 shown that a graphene–SiC waveguide behaves as a one-way 331 optical amplifier. Finally, it was demonstrated that a ring- 332 shaped graphene–SiC resonator can be used as spaser pumped 333 by the drifting electrons. 334

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at 337 <https://pubs.acs.org/doi/10.1021/acsp Photonics.0c01890>. 338

(A) The study of the influence of μ_c on the dispersion of 339 the current-driven SPPs and on the SPP field enhance- 340 ment, (B) derivation of the reflection and transmission 341 coefficients of the graphene–SiC system, (C) derivation 342 of the fields radiated by a linearly polarized emitter 343 placed near the graphene–SiC nanostructure, (D) 344

345 comparison of the growth rates predicted by different
346 graphene conductivity models, and (E) the study of the
347 influence of the relaxation time τ on the real part of the
348 drift-current biased graphene conductivity (PDF)

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362 Notes

363 The authors declare no competing financial interest.

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